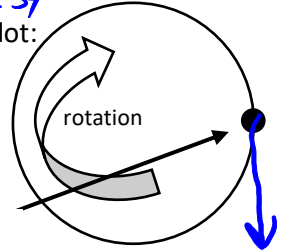


5.1 Circular Motion: Centripetal Acceleration

After watching Merry-Go-Round Fail compilations on YouTube, let's answer a few of these questions:
 (By the way, please don't do those stupid things at home. These were exactly the videos used in the TV show: Science of Stupid)

- 1) When did the people in the merry-go-round flew off the ride? when the merry-go-round was going fast
- 2) When they left the circle, which direction were they going? Complete the arrow on the black dot:
- 3) Why did these people flew off the ride at this point?

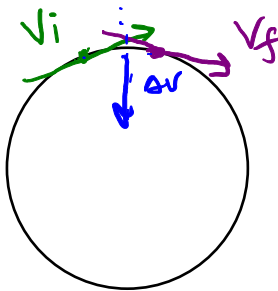
They did not apply enough force on the merry-go-round so the merry-go-round did not apply enough force on them.



Point when person flew off ride

Key point: there must be a net force acting on an object to keep it moving around in a circle. This net force must be directed towards the center of the circle.

Doesn't that mean that the object is accelerating towards the center of the circle? Why? Since an object's instantaneous velocity when moving around in a circle is tangent to the circle:



$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t} = \frac{v_f - v_i}{\Delta t}$$

$v \rightarrow$ speed (m/s)
 $r \rightarrow$ radius of circle (m)

$$a_c = \frac{v^2}{r} \quad (\text{m/s}^2)$$

We call this acceleration: centripetal acceleration (a_c).

The speed of an object in circular motion is since the circumference of the circle is $2\pi r$. $v = \frac{d}{t}$

$$v = \frac{2\pi r}{T} \quad (\text{m/s})$$

$T =$ period (s)
 \rightarrow time it takes the object to make 1 cycle

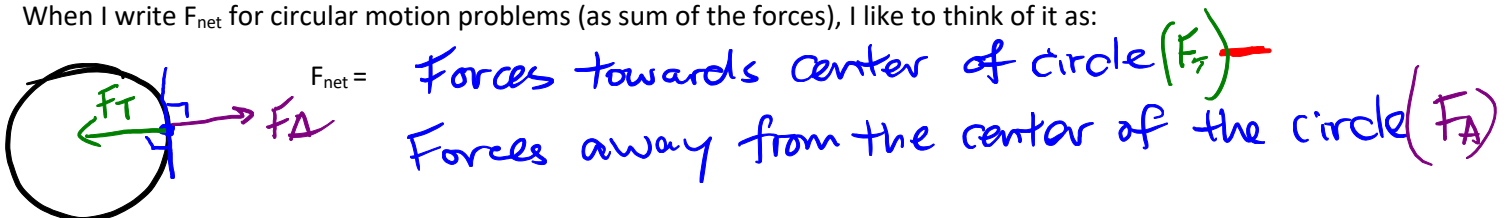
That means a_c can also be expressed as:

$$a_c = \frac{v^2}{r} = \left(\frac{2\pi r}{T}\right)^2 \frac{1}{r} = \frac{4\pi^2 r^2}{T^2 r} = \frac{4\pi^2 r}{T^2} \quad (\text{m/s}^2)$$

We can use Newton's 2nd Law: $F_{net} = ma$ to show that an object's (m) centripetal acceleration is proportional to the the sum of the forces **towards the center of the circle**.

$$F_{net} = ma = \frac{mv^2}{r} = m \left(\frac{4\pi^2 r}{T^2} \right)$$

When I write F_{net} for circular motion problems (as sum of the forces), I like to think of it as:



Name: _____

Below are some examples:

Ex 1: A plane makes a complete circle with a radius of 3622m in 2.10 min.

- a) What is the speed of the plane? (ANS: 181m/s)
- b) What is the centripetal acceleration of the plane? (ANS: 9.01m/s²)

$$a) \quad v = \frac{2\pi r}{T} = \frac{2\pi(3622m)}{2.10 \times 60} = \boxed{181m/s}$$

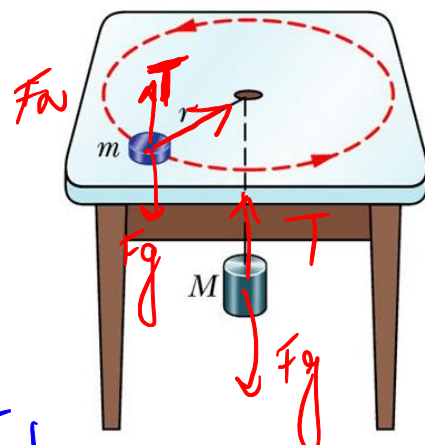
$$T = 2.10 \times 60$$

$$b) \quad a_c = \frac{v^2}{r} = \frac{(180...)^2}{(3622)} = \boxed{9.01m/s^2}$$

$$a) \quad F_{net} = T = \frac{mv^2}{r}$$

$$= \frac{0.5(2.3)^2}{0.2}$$

$$= \boxed{13N}$$

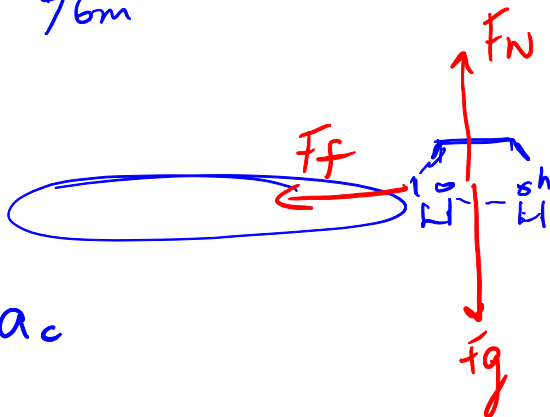


Ex. 2: A car is traveling at 14m/s around an unbanked (flat), curved road that has a radius of 96m.

- a) What is the centripetal acceleration? (ANS: 2.0 m/s²)
- b) What is the minimum coefficient of friction between the road and the car's tires? (ANS: 0.21)

$$a) \quad a_c = \frac{v^2}{r} = \frac{(14m/s)^2}{96m} = 2.0m/s^2$$

b)



$$F_{net} = F_f = ma_c$$

$$F_f = \mu F_N = \frac{\cancel{m}g}{g} = \frac{ma_c}{g}$$

$$\mu = \frac{a_c}{g} = \frac{2.0...}{9.8} = \boxed{0.21}$$

Ex. 3: A 0.50 kg mass (m) sits on a frictionless table and is attached via a string to a hanging weight (M) through a hole in the middle of the table. The 0.50 kg mass is whirled in a circle of radius 0.20m at 2.3m/s while the hanging weight is dangling underneath the table without falling onto the floor.

- a) Calculate the tension in the string. (ANS: 13N)
- b) Calculate the mass of the hanging weight. (ANS: 1.3kg)

$$\cancel{F_c} \rightarrow F_{net}$$

$$b) \quad F_g = T$$

$$\frac{T}{g} = \frac{Mg}{g}$$

$$F_N = F_g$$

$$M = \frac{13...}{9.8}$$

$$= \boxed{1.3kg}$$

HW: wkst 5.1

$$\cancel{F_c} \rightarrow F_{net}$$