

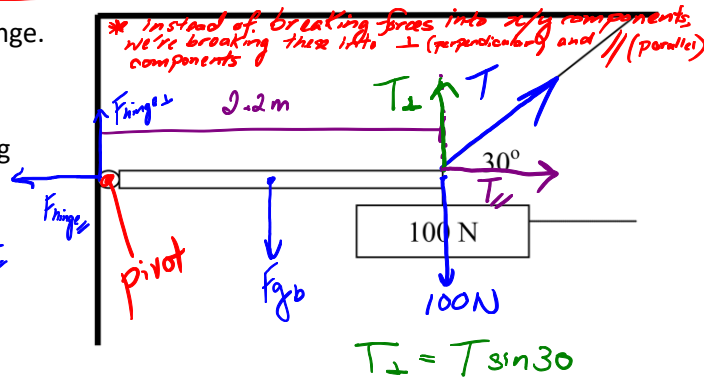
3.6 Torque (part 2)

Last class, we looked at torques caused by perpendicular forces acting on lever arms. What if these forces are **not** acting perpendicular on our lever arm?

Key point: we need to find the **component of the force acting perpendicular to the beam** and use this to find torque.

Ex. 1: A 2.2m long 50.0N uniform beam is attached to the wall by a hinge. A 100N weight is attached to the end of the uniform beam.

- a) What is the tension in the rope?
- b) What are the vertical and horizontal components of the supporting force provided by the hinge?



$\tau = F_{\perp}d$ $\sum F_y = 0$ $\sum F_x = 0$

a) $\sum \tau_{cw} = \sum \tau_{ccw}$ b) x direction: $F_{hx} = T_{\parallel}$

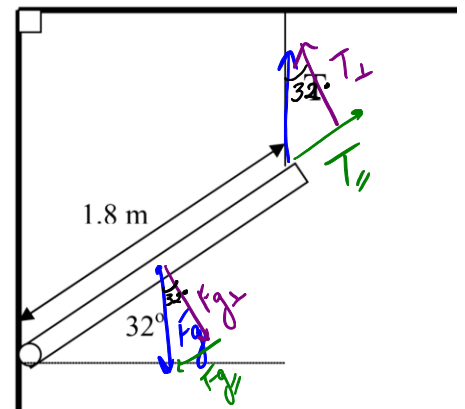
$\tau_b + \tau_{mass} = \tau_{tension}$

$F_{gb}(1.1) + 100(2.2) = T_{\perp}(2.2)$

$50.0(1.1) + 100(2.2) = T \sin 30(2.2)$

$T = \frac{50.0(1.1) + 100(2.2)}{\sin 30(2.2)} = \boxed{250N}$

Ex. 2: A 12.0kg uniform beam is attached to the ceiling by the rope shown on the right. What is the tension in the rope?



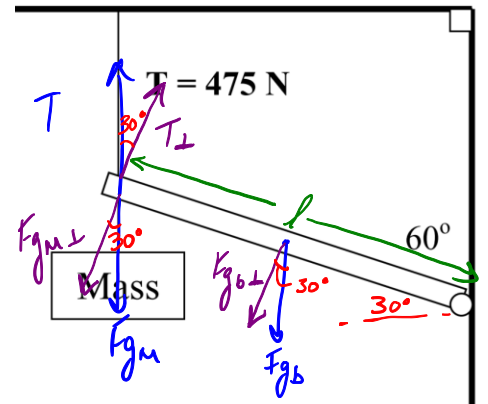
$\sum \tau_{cw} = \sum \tau_{ccw}$ $\tau = F_{\perp}d$

$T_{\perp}(1.8) = F_{g_{\perp}}(1.8)$

$T \cos 32(1.8) = mg \cos 32(1.8)$

$T = \frac{12(9.8) \cos 32(0.9)}{\cos 32(1.8)} = \boxed{59N}$

Ex. 3: A mass is tied to the very end of a 115N uniform beam. A rope is tied at the end of this beam and has a tension force of 475N. What is the mass tied to the end of this rope?



$\sum \tau_{cw} = \sum \tau_{ccw}$ $\tau = F_{\perp}d$

$T_{\perp}l = F_{g_{m\perp}}l + F_{g_{b\perp}}l$

$T \cos 30 = M g \cos 30 + \frac{m_b g \cos 30}{2}$

$\frac{T \cos 30 - m_b g \cos 30}{g \cos 30} = \frac{M g \cos 30}{g \cos 30}$

$M = \frac{T - m_b g / 2}{g} = \frac{475 - 115/2}{9.8} = \boxed{43kg}$